Introduction

Educational policymakers in most schools and districts face considerable pressure to improve student achievement. Principals and teachers recognize, and research confirms, that teachers vary considerably in their ability to improve student outcomes (Rivkin et al., 2005; Rockoff, 2004). Given the research on the differential impact of teachers and the vast expansion of student achievement testing, policy-makers are increasingly interested in how measures of teaching effectiveness, including but not limited to value-added, might be useful for improving the overall quality of the teacher workforce.

Some of these efforts focus on identifying high-quality teachers for rewards (Dee & Wyckoff, 2015), to take on more challenging assignments, or to serve as models of expert practice (Glazerman & Seifullah, 2012). Others attempt to identify struggling teachers in need of mentoring or professional development to improve skills (Taylor & Tyler, 2011; Yoon, 2007). Because some teachers may never become effective, some researchers and policymakers are exploring dismissals of ineffective teaches as a mechanism for improving the teacher workforce (Boyd, Lankford, Loeb, & Wyckoff, 2011; Goldhaber & Theobald, 2013; Winters & Cowen, 2013).

Interest in measuring teacher effectiveness persists throughout teachers' careers but is particularly salient during the first few years when potential benefits are greatest. Attrition of teachers is highest during these years (Boyd, Grossman, Lankford, Loeb, & Wyckoff, 2008), and the ability to reliably differentiate more effective from less effective teachers would help target retention efforts. Moreover, less effective, inexperienced teachers may be able to sufficiently improve to become effective than those with more experience. Targeting professional development to these teachers early allows benefits to be realized sooner and thus influence more

students. Finally, nearly all school districts review teachers for tenure early in their careers (many states make this determination by the end of a teacher's third year). Tenure decisions can be more beneficial for students if measures of teaching effectiveness are considered in the process (Loeb, Miller, & Wyckoff, 2014).

The benefits to policymakers of early identification of teacher effectiveness are clear; the ability of currently available measures to accurately do so is much less well understood. Indeed, teachers often voice doubts about school and district leaders' ability to capture teacher effectiveness using admittedly crude measures like value-added scores, intermittent observations, and/or principal evaluations. Their concerns are understandable, given that value-added scores are imprecise and districts are increasingly experimenting with linking important employment decisions to such measures, especially in the first few years of the career. A well-established literature examines the predictive validity of teacher value-added for all teachers, which suggests that there is some useful signal amongst the noise but the measures are imprecise for individual teachers (see e.g., McCaffrey, 2012). Somewhat surprisingly, there is very little research that explores the predictive validity of measures of teacher effectiveness for early career teachers, despite good reasons to believe the validity would differ by experience.

In this paper, we use value-added scores as one example of a measure of teaching effectiveness. We do so not because value-added measures capture all aspects of teaching that are important, nor because we think that value-added measures should be used in isolation. In fact, virtually all real-world policies that base personnel decisions on measures of teaching effectiveness combine multiple sources of information, including classroom observational rubrics, principal perceptions, or even student- and parent- surveys. Districts tend to use value-added measures (in combination with these other measures) when available, and because value-

added scores often vary more than other measures, they can be an important component in measures of teaching effectiveness (Donaldson & Papay, 2014; Kane, McCaffrey, Miller, & Staiger, 2013). We focus on value-added scores in this paper as an imperfect proxy for teaching effectiveness that is being used by policy-makers today. Understanding the properties of value-added for early career teachers is relevant in this policy context.

Measured value-added for novice teachers may be more prone to random error than for more experienced teachers as their value-added estimates are based on fewer years of data and fewer students. Moreover, novice teachers on average tend to improve during the first few years of their careers and thus their true effectiveness may change more across years than that for more experienced teachers. Figure 1 depicts returns to experience from eight studies, as well as our own estimates using data from New York City.[1] Each study shows increases in student achievement as teachers accumulate experience such that by a teacher's fifth year her or his students are performing, on average, from five to 15 percent of a standard deviation of student achievement higher than when he or she was a first year teacher.[2] However, little is known about the *variability* of early career returns to experience. If some teachers with similar initial performance improve substantially and others do not, early career effectiveness measures will be weak predictors of later performance.

This paper explores how well teacher performance, as measured by value-added over a teacher's first two years predicts future teacher performance. Toward this end we address the following two research questions: (1) Does the ability to predict future performance differ between novice and veteran teachers? (2) How well does initial job performance predict future performance? We conclude the paper with a more in-depth exploration of the policy implications and tradeoffs associated with inaccurate predictions.

This paper makes several contributions to existing literature on the use of measures of teaching effectiveness. Although an existing literature documents the instability of value-added (see, for example Goldhaber & Hansen, 2010a; Koedel & Betts, 2007; McCaffrey, Sass, Lockwood, & Mihaly, 2009), that literature largely does not distinguish between novice and veteran teachers and when it does (Goldhaber & Hansen, 2010b) the focus is specifically on tenure decisions. We build on this work, showing that value-added over the first two years is less predictive of future value-added than later in teachers' careers. Nonetheless, there is still signal in the noise; early performance is predictive of later performance. We also develop and illustrate a policy analytic framework that demonstrates the tradeoffs of employing imprecise estimates of teacher effectiveness (in this case, value-added) to make human resources policy decisions. How policy makers should use these measures depends on the policy costs of mistakenly identifying a teacher as low or high performing when the teacher is not, versus the cost of not identifying a teacher when the identification would be accurate.

Background and Prior Literature

Research documents substantial impact of assignment to a high-quality teacher on student achievement (Aaronson et al., 2007; Boyd, Lankford, Loeb, Ronfeldt, & Wyckoff, 2011; Clotfelter et al., 2007; Hanushek, 1971; Hanushek, Kain, O'Brien, & Rivkin, 2005; Harris & Sass, 2011; Murnane & Phillips, 1981; Rockoff, 2004). The difference between effective and ineffective teachers affects proximal outcomes like standardized test scores, as well as distal outcomes such as college attendance, wages, housing quality, family planning, and retirement savings (Chetty, Friedman, & Rockoff, 2011).

Given the growing recognition of the differential impacts of teachers, policy-makers are increasingly interested in how measures of teacher effectiveness such as value-added or structured observational measures might be useful for improving the overall quality of the teacher workforce. The Measures of Effective Teaching (MET Project), Ohio's Teacher Evaluation System (TES), and D.C.'s IMPACT policy are all examples where value-added scores are considered in conjunction with other evidence from the classroom, such as observational protocols or principal assessments, to inform policy discussions aimed at improving teaching.

The utility of teacher effectiveness measures for policy use depends on properties of the measures themselves, such as validity and reliability. Measurement work on the reliability of teacher value-added scores has typically used a test-retest reliability perspective, in which a test administered twice within a short time period is judged based on the equivalence of the results over time. Researchers have thus examined the stability of value-added scores across proximal years, reasoning that a reliable measure should be consistent with itself from one year to the next (Aaronson et al., 2007; Goldhaber & Hansen, 2010a; Kane & Staiger, 2002; Koedel & Betts, 2007; McCaffrey et al., 2009). When value-added scores fluctuate dramatically in adjacent years, this presents a policy challenge—the measures may reflect statistical imprecision (noise) more than true teacher performance. In this sense, stability is a highly desirable property in a measure of effectiveness, because measured effectiveness in one year predicts well effectiveness in subsequent years. Lockwood, Louis, and McCaffrey (2002) use simulations to explore how precise measures of performance would need to be to support inferences even at the tails of the distributions of teaching effectiveness, and find that the necessary signal-to-noise ratio is perhaps unrealistically high. Schochet and Chiang (2013) also point out that the unreliability of teacher

value-added estimates would lead to errors in identification of effective/ ineffective teachers. They estimate error rates of about 25 percent among teachers of all experience levels when comparing teacher performance to that of the average teacher. However, neither paper focuses on differences between early career teachers and other teachers.

The perspective that stability and reliability are closely connected makes sense when true teaching effectiveness is expected to be relatively constant, as is the case of mid-career and veteran teachers. However, as shown above in Figure 1, the effectiveness of early career teachers substantially changes over the first five years of teaching. Thus, teacher quality measures may reflect rue changes over this period and, as a result, their measures could change from year to year in unpredictable ways. Anecdotally, one often hears that the first two years of teaching are a "blur," and that virtually every teacher feels overwhelmed and ineffective. If, in fact, first-year teachers' effectiveness is more subject to random influences and less a reflection of their true long-run abilities, their early evaluations would be less predictive of future performance than evaluations later in their career and would not be a good source of information for long-term decision making. Alternatively, even though value-added tends to meaningfully improve for early career teachers, teachers' initial value-added may predict their value-added in the future quite well and thus be a good source of information for decision making.

We are aware of two related papers that explicitly focus on the early career period. Goldhaber and Hansen (2010b) explore the feasibility of using value-added scores in tenure decisions by running models that predict future student achievement as a function of teacher pre-tenure value-added estimates versus traditional teacher characteristics such as experience, master's degree obtainment, licensure scores, and college selectivity, and find that the value-added scores are just as predictive as the full set of teacher covariates. We build upon this work

by exploring in more depth the implications of error in early career value-added scores for teachers. We model average trends in value-added scores by quintile of initial performance to examine propensity for improvement, and we explore the extent to which quintiles of initial performance overlap with quintiles of future performance. Staiger and Rockoff (2010) conduct Monte Carlo simulations to explore the feasibility of making early career decisions with information of varying degrees of imprecision. For example, they examine the possibility of dismissing some proportion of teachers after their *first* year on the job and find that it would optimize mean teacher performance to dismiss 80 percent of teachers after their first year—a surprisingly high threshold, though it does not account for possible effects on non-dismissed teachers on the pool of available teacher candidates.

The current paper distinguishes itself by providing an in-depth analysis of the real-world predictive validity of value-added, with a distinct focus on teachers at the start of their career—a time when teacher performance is changing most rapidly and when districts have the greatest leverage to implement targeted human resource interventions and decisions. This paper explores how actual value-added scores from new teachers' first two years would perform in practice if used by policy makers to anticipate and shape the future effectiveness of their teaching force. We are particularly interested in providing a framework through which policy makers might think about relevant policy design issues relative to current practice in most districts. Such issues include: what is an appropriate threshold for initial identification as highly effective or in-need of intervention; how much overlap is there in the future performance of initially highly effective and ineffective teachers; what are the tradeoffs as one considers identifying more teachers as ineffective early in the career. We consider these questions in terms of early identification of both highly effective teachers (to whom districts might want to target retention efforts), as well

as ineffective teachers (to whom the district might want to target additional support). Finally, we explore whether value-added scores in different subjects might be more or less useful for early identification policies—an issue not covered to date with regard to early career teachers but one that turns out to be important (see, Lefgren and Sims (2012) for an analysis of using cross-subject value-added information for teachers of all levels of experience in North Carolina).

Data

The backbone of the data used for this analysis is administrative records from a range of sources including the New York City Department of Education (NYCDOE) and the New York State Education Department (NYSED). These data include annual student achievement in math and English Language Arts (ELA) and the link between teachers and students needed to create measures of teacher effectiveness and growth over time.

New York City students take achievement exams in math and ELA in grades three through eight. However, for the current analysis, we restrict the sample to value-added for elementary school teachers (grades four and five), because of the relative uniformity of elementary school teaching jobs compared with middle school teaching where teachers typically specialize. All the exams are aligned to the New York State learning standards and each set of tests is scaled to reflect item difficulty and are equated across grades and over time. Tests are given to all registered students with limited accommodations and exclusions. Thus, for nearly all students the tests provide a consistent assessment of achievement from grade three through grade eight. For most years, the data include scores for 65,000 to 80,000 students in each grade. We standardize all student achievement scores by subject, grade and year to have a mean of zero and a unit standard deviation. Using these data, we construct a set of records with a student's current

exam score and lagged exam score(s). The student data also include measures of gender, ethnicity, language spoken at home, free-lunch status, special-education status, number of absences in the prior year, and number of suspensions in the prior year for each student who was active in any of grades three through eight in a given year. Data on teachers includes teacher race, ethnicity, experience, and school assignment as well as a link to the classroom(s) in which that teach taught each year.

Analytic Sample and Attrition

The paper explores how measures of teacher effectiveness—value-added scores—change during the first five years of a teacher's career. For this analysis, we estimate teacher value-added for the subset of teachers assigned to tested grades and subjects. Because we analyze patterns in value-added scores over the course of the first five years of a teacher's career, we can only include teachers who do not leave teaching before their later performance can be observed. Teachers with value-added scores typically represent about 20 percent of all teachers, somewhat more among elementary school teachers and less in other grades. As we indicate elsewhere, our analysis is intended to be illustrative of a process that could employ other measures of teacher effectiveness.

Table 1 provides a summary of three relevant analytic samples (by subject) and their average characteristics in terms of teacher initial value-added scores, demographics, and prior training factors including SAT scores, competitiveness of their undergraduate institution, and pathway into teaching. In the relevant school years for this study, we observe 3,360 elementary school teachers who have a value-added score in their first year of teaching (3,307 for ELA). This is the population of interest—group (A) in Table 1. Of these, about 29 percent (966 teachers) have value-added scores in *all* of the following four years, allowing us to track their

long-run effectiveness annually. This sample—group (C) in Table 1—becomes our primary analytic sample for the paper. Limiting the sample to teachers with five consecutive years of value-added addresses a possible attrition problem, wherein any differences in future mean group performance could be a result of a systematic relationship between early performance and the decision to leave within the first five years. The attrition of teachers from the sample may threaten the validity of the estimates as prior research shows evidence that early attriters can differ in effectiveness, and, thus maybe in their returns to experience (Boyd et al., 2007; Goldhaber, Gross, & Player, 2011; Hanushek et al., 2005). As a result, our primary analyses focus on the set of New York City elementary teachers who began between 2000 and 2007 who have value-added scores in all of their first five years (N=966 for math, N= 972 for ELA).

Despite the advantages of limiting the sample in this way, the restriction of possessing value-added scores in every year introduces a potential problem of external validity. The notable decrease in sample size from group (A) to group (C) reveals that teachers generally do not receive value-added scores in every school year, and in research presented elsewhere we examine this phenomenon (Atteberry, Loeb, Wyckoff, 2013). That paper shows there is substantial movement of teachers in an out of tested grades and subjects. Some of this movement may be identified as strategic—less effective teachers are moved out of tested grades and subjects. However, many of these movements appear less purposeful and therefore may reflect inevitable random movement in a large personnel management system. If teachers who are less effective leave teaching or are moved from tested subjects or grades during their first five years, the estimates of mean value-added would be biased upward. That is, teachers who are consistently assigned to tested subjects and grades for five consecutive years may be different from those who are not. Because the requirement of having five consecutive years of value-

added scores is restrictive, we also examine results using a larger subsample of New York City teachers who have value-added scores in their first year and two of the following four years. This is group (B) in Table 1 (n=2,333 teachers for math, 2,298 teachers for ELA). By using this larger subsample, we can run robustness checks using 70.1 percent of the 3,360 elementary teachers who have value-added scores in their first year (rather than the 28 percent when we use group (A)). Table 1 shows that the average value-added scores, demographics, and training of teachers in these three groups are quite similar to one another, with few discernable patterns. In addition, while the primary analytic sample for the paper is group (A), we also replicate our primary analyses using group (B) in Appendix C and find that the results are qualitatively very similar.

Methods

The analytic approach in this paper is to follow a panel of new teachers through their first five years and retrospectively examine how performance in the first two years predicts performance thereafter. We estimate yearly value-added scores for New York City teachers in tested grades and subjects. We then use these value-added scores to characterize teachers' developing effectiveness over the first five years of their careers to answer the research questions outlined above. We begin by describing the methods used to estimate teacher-by-year value-added scores, and then describe how these scores are used in the analysis.

Estimation of Value Added

Although there is no consensus about how best to measure teacher quality, this paper defines teacher effectiveness using a value-added framework in which teachers are judged by their ability to stimulate student standardized test score gains. While imperfect, these measures have the benefit of directly measuring student learning, and they have been found to be

predictive of other measures of teacher effectiveness such as principals' assessments and observational measures of teaching practice (Atteberry, 2011; Grossman et al., 2010; Jacob & Lefgren, 2008; Kane & Staiger, 2012; Kane, Taylor, Tyler, & Wooten, 2011; Milanowski, 2004), as well as long term student outcomes (Chetty et al., 2011). Our methods for estimating teacher value-added are consistent with the prior literature. We estimate teacher-by-year value-added employing a multi-step residual-based method similar to that employed by the University of Wisconsin's Value-Added Research Center (VARC). VARC estimates value-added for several school districts, including until quite recently New York City (see Appendix B). In Appendix C, we also examine results using two alternative value-added models to the one used in the paper. "VA Model B" uses a gain score approach rather than the lagged achievement approach used in the paper. "VA Model C" differs from the main value-added model described in the paper in that it uses student-fixed effects in place of time-invariant student covariates such as race/ ethnicity, gender, etc. In future work, others may be interested in whether teacher effectiveness measures derived from student growth percentile models would also garner similar results.

RQ 1. Does the ability to predict future performance differ between novice and veteran teachers?

Previous research frequently characterizes the predictiveness of future value-added based on current value-added by examining correlations between the two or by examining the stability of observations along the main diagonal of a matrix of current and future performance quintiles. Although we explore other measures of predictiveness below, we employ these measures to assess whether there are meaningful differences between predictiveness of novice and veteran teachers.

RQ 2. How well does initial job performance predict future performance?

The relationship between initial and future performance may be characterized in several ways. We begin by estimating mean value-added score trajectories during the first five years separately by quintiles of teachers' initial performance. We do so by modeling the teacher-by-year value-added measures generated by Equation 1 as outcomes using a non-parametric function of experience with interactions for initial quintile. Policy makers often translate raw evaluation scores into multiple performance groups in order to facilitate direct action for top and bottom performers. We also adopt this general approach for characterizing early career performance for a given teacher for many of our analyses. The creation of such quintiles, however, requires analytic decisions that we delineate in Appendix A.

Mean quintile performance may obscure the variability that exists within and across quintiles. For this reason, we estimate regression models that predict a teacher's continuous value-added score in a future period as a function of a set of her value-added scores in the first two years of teaching. We use Equation 2 to predict each teacher's value-added score in a given "future" year (e.g., value-added score in years three, four, five, or the mean of these) as a function of value-added scores observed in the first and second year. We present results across a number of value-added outcomes and sets of early career value-added scores, however Equation 2 describes the fullest specification which includes a cubic polynomial function of all available value-added data in both subjects from teachers' first two years:

$$E[VA_{m,y=3,4,5}] = \beta_0 + f^3(VA_{m,y=1}) + f^3(VA_{m,y=2}) + f^3(VA_{e,y=1}) + f^3(VA_{e,y=2}) \tag{2}$$

Equation 2 shows a teacher's math value-added score averaged in years 3, 4, and 5, $E[VA_{m,y=3,4,5}]$, predicted based on a cubic function, f^3, of the teacher's math value-added scores from years 1 and 2, $(VA_{m,y=1})$ and $(VA_{m,y=2})$, as well as ELA value-added scores from years 1 and 2 $(VA_{e,y=1})$ and $(VA_{e,y=2})$. We summarize results from forty different permutations

of Equation 2—by subject and by various combinations of value-added scores used—by presenting the adjusted R-squared values that summarize the proportion of variance in future performance that can be accounted for using early value-added scores.

As policymakers work to structure an effective teaching workforce they typically want to understand whether early career teachers will meet performance standards that place them in performance bands, such as highly effective, effective, or ineffective. Even if the proportion of the variance of future performance explained by early performance is low, it may be still be a reliable predictor of these performance bands. We examine this perspective by examining mobility across performance levels of a quintile transition matrix of early and later career performance. For example, how frequently do initially high (low) performing teachers become low (high) performing teaches?

Finally we examine the distribution of future performance scores separately by quintiles of initial performance. To the extent that these distributions are distinct from one another, it suggests that the initial performance quintiles accurately predict future performance.

Policy Implications and Tradeoffs Associated with Inaccurate Predictions

Because we know that errors in prediction are inevitable, we present evidence on the nature of misidentification based on value-added scores from a teacher's first two years. We present a framework for thinking about the kinds of mistakes likely to be made and for whom those mistakes are costly, and we apply this framework to the data from New York City. We propose a hypothetical policy mechanism in which value-added scores from the early career are used to rank teachers and identify the strongest or weakest for any given human capital response (e.g., targeted professional development, tenure decisions, or performance incentives). We then follow teachers through their fifth year, examining the frequency of accurate and inaccurate

identifications based on early career designations. We use this approach to assess the benefits and costs of employing early career measures of value-added to predict future value-added. In addition, we examine whether such early career identification policies differentially affect teachers by race and ethnicity.

Results

RQ 1. Does the ability to predict future performance differ between novice and veteran teachers?

The value-added of novice teachers is less predictive of future performance than is value-added of veteran teachers. Table 2 shows the correlations of value-added of first-year teachers with their value-added in successive years as well as the correlation of value-added of teachers with at least six years of experience with their value-added in successive years. In all cases value-added is single year value added. In math, the correlations for novice teachers are always smaller than those for experienced teachers (differences are always statistically significant). Most relevant for our purposes is that the correlations with out-year value-added diminish much more rapidly for novice than experienced teachers. For example, the correlation in "Year + 5" is 37 percent of that in "Year + 1" for novice teachers (0.132 vs. 0.356), while it is 75 percent for veteran teachers (0.321 vs. 0.421). A similar, though somewhat less consistent and diminished pattern exists in ELA. Value-added for early career teachers is meaningfully less predictive of future value-added than it is for more experienced teachers. As we noted above, there is great conceptual appeal to employing value-added in a variety of policy contexts for early career teachers. Just how misleading is early career value-added of future performance? How might this affect policy decisions? We explore these questions below.

RQ 2. How well does initial job performance predict future performance?

Teachers with comparable experience can vary substantially in their effectiveness. For example, we estimate the standard deviation in teacher math value-added of first-year teachers is 0.21. Twenty percent of a standard deviation in student achievement is large relative to most educational interventions (Hill, Bloom, Black, & Lipsey, 2008) and produces meaningful differences in long term outcomes for students (Chetty, Friedman, & Rockoff, 2014). Does this variability in early career performance predict future differences? We assess the stability of early career differences from a variety of perspectives.

Figure 2 provides evidence of consistent differences in value-added across quintiles of initial performance.[3] Although the lowest quintile does exhibit the most improvement (some of which may be partly due regression to the mean), this set of teachers does not, on average, "catch up" with other quintiles, nor notably are they typically as strong as the median first-year teacher even after five years. The issue of regression to the mean is somewhat mitigated by our choice to characterize initial performance by the mean value-added score in the first two years. In order to check the robustness of our findings to some of our main analytic choices, in Appendix C, we recreate Figure 2 across three dimensions: (A) minimum value-added required for inclusion in the sample, (B) how we defined initial quintiles, and (C) specification of the value-added models used to estimate teacher effects. Findings are quite similar in general pattern, suggesting that these results hold up whether we use the less-restrictive subset of teachers (based on number of available value-added scores), or had used other forms of the value-added model.

While useful for characterizing the mean pattern in each quintile, Figure 2 potentially masks meaningful within-quintile variability. To explore this issue we present adjusted R-squared values from various specifications of Equation 2 above in Table 3. This approach uses the full continuous range of value-added scores and does not rely on quintile definitions and their

arbitrary boundaries. One evident pattern is that additional years of value-added predictors improve the predictions of future value-added—particularly the difference between having one score and having two scores. For example, teachers' math value-added scores in the first year explain 7.9 percent of the variance in value-added scores in the third year. The predictive power is even lower for ELA (2.5 percent). Employing value-added for the first two years explains 17.6 percent of value-added in the third year (6.8 percent for ELA). A second evident pattern in Table 3 is that value-added scores from the second year are typically two- to three times stronger predictors than value-added in the first year for both math and ELA.

Recall that elementary school teachers typically teach both math and ELA every year and thus we can estimate both a math and an ELA score for each teacher in each year. When we employ math value added in both of the first two years we explain slightly more than a quarter of the variation in future math value-added averaged across years 3 through 5 (0.256). Adding reading value-added improves the explanatory power, but not by much (0.262).

The predictive power of early value-added measures depends on which future value-added measure they are predicting. Not surprisingly, given the salience of measurement error in any given year, early scores explain *averaged* future scores better than they explain future scores in a particular year. For example, for math, our best prediction model for year 3 value-added (column 1) explains only 17.6 percent of the variation (8.5 percent for ELA). In contrast, when predicting variation in mean performance across years three through five (column 4), the best model predicts up to about 26 percent of the variance in math (16.8 percent in ELA).

Teacher's early value-added is clearly an imperfect predictor of future value-added. To benchmark these estimates, we compare them to predictiveness of other characteristics of early career teachers and to other commonly employed performance measures. As one comparison, we

estimate the predictive ability of measured characteristics of teachers during their early years. These include typically available measures: indicators of a teacher's pathway into teaching, available credentialing scores and SAT scores, competiveness of undergraduate institution, teacher's race/ethnicity, and gender. When we predict math mean value-added scores in years three through five (same outcome as column 4 of Table 3) using this set of explanatory factors, we explain less than 3 percent of the variation in the math or ELA outcomes.[4] Another way of benchmarking these findings is to compare them to the predictive validity of other commonly accepted measures used for high-stakes evaluation. For example, SAT scores, often employed in decisions to predict college performance and grant admission, account for about 28 percent of the variation in first-year college GPA (Mattern & Patterson, 2014). For a non-education example, surgeons and hospitals are also often rated based on factors that are only modestly correlated with patient mortality (well below 0.5), however the field publishes these imperfect measures because they are better than other available approaches to assessing quality (Thomas & Hofer, 1999). (See also Sturman, Cheramie, & Cashen, 2005 for a meta-analysis of the temporal consistency of performance measures across different fields). Although early career value-added is far from a perfect predictor of future value-added, it is far better than other readily available measures of teacher performance and is roughly comparable to the SAT as a predictor of future college performance.

These analyses suggest that initial value-added is predictive of future value-added; however, they also imply that accounting for the variance in future performance is difficult. Each of the prior illustrations provides useful information but also have shortcomings: The mean improvement trajectories by quintile shown above in Figure 2 may obscure the mobility of teachers across quintiles. The explained variation measures reported in Table 3 provide much

more detailed information regarding the relationship between early and future performance but may not inform a typical question confronting policymakers—how frequently do teachers assigned to performance bands, e.g., high or low performing, based on initial value-added remain in these bands when measured by future performance?

To illustrate the potential of value-added to address this type of question, Table 4 shows a transition matrix that tabulates the number of teachers in each quintile of initial performance (mean value added of years 1 and 2) (rows) by how those teachers were distributed in the quintiles of future performance (mean value-added of years 3 through 5) (columns), along with row percentages.[5] The majority—62 percent—of the initially lowest quintile math teachers are in the bottom two quintiles of future performance. Thus a teacher initially identified as low-performing is quite likely to remain relatively low-performing in the future. About 69 percent of initially top quintile teachers remain in the top two quintiles of mean math performance in the following years. Results for ELA are more muted: About 54 percent of the initially lowest quintile are in the bottom two quintiles in the future, and 60 percent of the initially highest quintile remain in the top two quintiles in the future. Overall, the transition matrix suggests that measures of value-added in the first two years predict future performance for most teachers, although the future performance of a sizeable minority of teachers may be mischaracterized by their initial performance.

Broadening the transition matrix approach, we plot the distribution of future teacher effectiveness for each of the quintiles of initial performance (Figure 3). These depictions provide a more complete sense of how groups based on initial effectiveness overlap in the future.[6] The advantage, over the transition matrix shown above, is to illustrate the range of overlapping skills for members of the initial quintile groups. We can examine these distribution with various key

comparison points in mind. For each group, we have added two reference points, which are helpful for thinking critically about the implications of these distributions relative to one another. First, the "+" sign located on each distribution represents the mean future performance in each respective initial-quintile group. Second, the diamond ("♦") represents the mean *initial* performance by quintile. This allows the reader to compare distributions both to where the group started on average, as well as to the mean future performance of each quintile.

The vast majority of policy proposals based on value-added target teachers at the top (for rewards, mentoring roles, etc.) or at the bottom (for support, professional development, or dismissal). Thus, even though the middle quintiles are not particularly distinct in Figure 3, it is most relevant that the top and bottom initial quintiles are. In both math and ELA, there is some overlap of the extreme quintiles in the middle—some of the initially lowest-performing teachers are just as skilled in future years as initially highest-performing teachers. However, the large majority of these two distributions are distinct from one another.

How do the mischaracterizations implied by initial performance quintiles (Figure 3) compare to meaningful benchmarks? For example in math, 69 percent of the future performance distribution for the initially lowest performing quintile lies to the left of the mean performance of a new teacher (the comparable percentage is 67 percent for ELA). Thus, the future performance of more than two-thirds of the initially lowest performing quintile does not rise to match the performance of a typical new teacher. A more policy relevant comparison would likely employ smaller groupings of teachers than the quintiles described here.[7] We examine the mischaracterizations and the loss function for such a policy below.

Policy Implications: What are the Tradeoffs Associated with Inaccurate Predictions?

District leaders may want to use predictions of future effectiveness to assign teachers to various policy regimes for a variety of reasons. For example, assigning targeted professional development and support to early career teachers who are struggling represents potentially effective human resources policy. Another possibility would be to delay tenure decisions for teachers who have not demonstrated their ability to improve student outcomes during their first two years. Alternatively, if high-performing teachers could be identified early in their careers, just when attrition is highest, district and school leaders could target intensive retention efforts on these teachers. In our analysis, initial performance is a meaningful signal of future performance for many teachers; however, the future performance of a number of other teachers is not reflected well by their initial performance. What does this imprecision imply about the policy usefulness of employing initial value-added performance to characterize teacher effectiveness?

Figure 4 provides a framework for empirically exploring the potential tradeoffs in identifying teachers when the measures employed imprecisely identify teachers. It plots future performance as a function of initial performance percentiles. Moving from left to right along the x-axis represents an increase in the threshold for identifying a teacher as ineffective (i.e., candidates for intervention) based on initial performance. For this exercise, we capture initial performance by calculating the mean of a teacher's value-added scores in years one and two and translating that into percentiles (x-axis). The y-axis depicts the associated percentage of teachers who appear in each tercile of future performance.[8] The figure plots the extent to which those initially identified as low performing are in the bottom third of future performance (red portion), are in the middle (yellow), or are among the top third of future performance (green). It is, of course, somewhat arbitrary to use "bottom third" as the cutoff for teachers who continue to be

low-performing in the future. Below, we also explore defining a teacher as low-performing if he/she continues to perform below the average teacher (or the average first year teacher)—an approach that would identify more teachers as ineffective. Of these two options, we begin with our somewhat more conservative definition of relatively low-performing in the future (i.e., bottom third).

To illustrate the utility of this figure, we begin by focusing on the vertical line that passes through X=5 on the horizontal axis, which indicates the effects of identifying the lowest 5 percent of teachers as ineffective. In this first example, we are considering a proposal to move from a current policy where no teachers are identified as ineffective to a new policy in which the bottom 5 percent of the initial performance distribution are identified as ineffective.[9] For instance, those 5 percent of the initially lowest-performing teachers could receive targeted professional development in the early career. Does such a move constitute a policy improvement? We know the new policy will misidentify some teachers who are not low-performing in the future, and Figure 4 allows us to quantify that rate of misidentification. At that level (X=5), 75 percent (red) of teachers initially identified as ineffective subsequently perform in the lowest third of future performers. In other words, for three-fourths of the initially-identified set of teachers, the professional development intervention would have been warranted given that they continued to struggle into their fifth year. On the other hand, 16.7 percent of the initially-identified teachers are in the middle tercile of future performance (yellow), and 8.3 percent (green) end up in the top third of future performance. In this hypothetical scenario, the middle- and high- tercile teachers would therefore receive targeted professional development that they may not have needed because they would have moved out of the bottom third without it.[10]

In our first example, about a quarter of the 5 percent of teachers initially identified as low-performing are not among the bottom third in the future, and about 8 percent are actually among the most effective teachers in the future. It is worth keeping in mind here that this misidentification occurs for 8 percent *of the bottom 5 percent* of the overall distribution of teachers—that is, if there were 1000 teachers, 50 would have been initially identified as low-performing, and 4 of those would have subsequently appeared in the top tercile. The 5 percent threshold therefore made some—but not very many—egregious errors, in which teachers who would become among the most effective would have been inappropriately identified based on their early career value-added scores. On the flip side, we also know that 75 percent of the time the ineffective label correctly identifies teachers who will be low-performing in the future. Depending on the consequences, the identification process may accrue benefits to identified teachers, non-identified teachers, or students. It is important to compare this to the original policy in which no teachers were identified as ineffective. While the percentage of initially-identified teachers who are ultimately *mis*identified goes from 0 to 8 percent (the original policy vs. new 5 percent policy), we also know that the original policy failed to identify *any* teachers correctly,[11] whereas the new policy accurately captured future performance for 75 percent of teachers. This latter aspect of the policy comparison is often overlooked, since we are often more concerned with what could go wrong (for teachers) than what could go right (for students).

Thus far, we have examined findings at the 5 percent identification level, but we will see that future misidentification rates depend on the size of the initially-identified group. Figure 4 allows one to compare any two potential identification policies. If instead of identifying the bottom 5 percent of initial performers, one identifies the bottom 10 percent, the proportion of identified teachers who fall in the bottom tercile of future performance declines to 62.7 percent,

with the attendant increase in serious misclassification from 8.3 to 13.3 percent. The 10-percent identification policy is getting more predictions right than wrong, but the error rate is somewhat higher. One might be concerned that a 10 percent identification rate is unrealistically high, however we argue that it depends on the policy one has in mind. For instance, if considering a proportion of teachers to dismiss, 10 percent seems high given the high cost to teachers of this misidentification. However if considering a policy to target professional development to teachers who are struggling, misidentification has very little cost and therefore 10 percent may be appropriate.

The framework we present here is useful for examining the differential rates of accurate and inaccurate identification at different initial levels of early identification. As we discuss below, district leaders and policy makers must then think through the potential costs of misidentification and benefits of accurate identification that would be associated with whatever policy response they may be considering. In the case of targeting professional development, the costs to misidentification (a small percentage of teachers receiving PD they do not need) may not be particularly high. Indeed, it is common practice in districts for *all* teachers to receive professional development without regard to their performance. However, if the targeted policy intervention was, instead, delaying tenure (thus opening up the possibility that the teacher might not ultimately be retained), then the costs to misidentification would certainly be higher. Ultimately, the question of costs and benefits is policy- and context-specific. The information provided by our analysis can help policy makers think about the frequency of accurate predictions, but not the relative utility of those judgments.

Above we have walked through the results on the left-hand side of Figure 4 (math), however the empirical outcomes for ELA are substantively different. As shown in the second

panel of Figure 4, identifying ineffective teachers based on the lowest 5 percent of initial ELA performance leads to only 52.8 percent of these teachers being in the lowest tercile of future performance, implying that 47 percent are *not* among the bottom third in the long run (11.1 percent become among the top third of teachers in the future). Thus employing initial value-added to identify the future performance of teachers based on ELA value-added leads to many more misidentifications. This pattern is entirely consistent with our earlier analysis that showed future ELA effectiveness was less predictive than math effectiveness. As is evident, for ELA extending identification beyond six percent of teachers leads to more misidentified than correctly identified teachers. Again, how problematic this is depends on the benefits of correct identification and the costs of misidentification.

In Figure 4, we opted to think of future low-performance as continued presence in the bottom third of the distribution of teaching, however districts may have different thresholds for evaluating whether a teacher should be identified as low-performing. For example, let us consider a very different policy mechanism in which initially-identified teachers become candidates for dismissal. In this case, the relevant comparison would be between the identified teachers and the teacher who likely would be hired in her place—an average first year teacher. We therefore also compare a novice teacher's ongoing performance to that of an average first year teacher, as this represents an individual that could serve as a feasible replacement. In fact, among the teachers in the bottom 5 percent of the initial math performance distribution, the vast majority—83.3 percent—do not perform in the future as well as an average first year teacher in math. The corresponding number is 72.2 percent for ELA. In other words, had students who were assigned to these initially lowest-performing teachers instead been assigned to an average new teacher, they would have performed at higher levels on their end-of-year tests.

More concretely, the average math value-added score of a third-year teacher who initially performed in the bottom 5 percent in years one and two is about -0.15 standard deviation units. The average first-year teacher, on the other hand, has a math value-added score of -0.03 standard deviation units. The difference between the two is two-thirds of full standard deviation in teacher effectiveness. We therefore expect a large negative difference (around 0.11 standard deviations) in the potential outcomes for students assigned to these initially very low-performing teachers as opposed to an average new teacher, even in the third year alone. Further, an ineffective teacher retained for *three* additional years imposes three years of below-average performance on students. The longer a teacher with low true impacts on students is retained, the expected differential impact on students will be the *sum* of the difference between an average new teacher and the less effective teacher across years of additional retention.

The same logic can be applied to teachers at the high end of the teacher effectiveness spectrum. The average math value-added score of a third-year teacher who initially performed in the top five percent in years one and two is 0.24 standard deviation units. Imagine a scenario in which a school system cannot manage to retain this high-performing teacher, and as a result the students who would have been assigned to this teacher are instead assigned to her replacement—an average first year teacher (who would typically have a mean math value-added score of -0.03 standard deviation units). The impacts for these students would be dramatic in magnitude.

Accurately identifying the effectiveness of early career teachers has large benefits to improving educational outcomes for students. Misidentifying teacher effectiveness has potentially large costs for teachers and in some cases students. The analysis has shown how misclassifying teachers increases as the portion of teachers initially identified increases. What is the "right" level of identification? The answer is complex and depends on several factors. First,

as the current debate would imply, the predictiveness of future effectiveness by initial effectiveness is important. If initial value-added were a perfect predictor of future value-added, most policymakers would be much more comfortable with using it. Predictiveness also requires a clear criterion for identifying future ineffectiveness and excellence. Would policymakers be willing to agree that a teacher identified as initially high-performing was correctly identified as long as she was in the top tercile of future performance, as we have employed here? The smaller the future performance band, the less predictive any measure will be. Second, value-added measures of future performance are imprecise, narrowly defined and relative. Where possible, we mitigate the problems of measurement error by employing Bayes shrunk estimates as well as averaging across multiple future years. We, however, cannot address the narrowness of the value-added measure relative to the way most people conceptualize student outcomes, nor its relative nature. For these purposes employing multiple measures of teacher effectiveness—e.g., value-added augmented by rigorous observation protocols and other measures—would increase reliability and broaden the domains that are measured.

Third, tolerance for imprecision in identifying teachers also depends on the benefits of correct identification and the costs of misidentification. For example, if the benefit to students from more effective teachers was substantial, as suggested by Chetty et al. (2011) in terms of college-going and future earnings (for instance, they estimate that having a top 5 percent teacher for just one year raises a child's lifetime income by $80,000), that would imply an increased tolerance of the misclassification of increasing the identification of ineffective teachers, other things equal. As the district becomes known for rewarding effectiveness and intervening to help teachers who under-perform, teachers who think they can be rewarded in such a system may be attracted to the profession. On the other hand, if these identification systems seem to teachers to

be driven by noise and—due to the imprecision of any given measures of teaching effectiveness—and teachers do not perceive that these early identifications are reliable, then even effective teachers may be discouraged from remaining in the profession. Little is known about how increasing the link between imperfect teacher performance measures and teacher pay or retention policies would affect the general equilibrium of the teacher labor market, however Rothstein (forthcoming) explores these issues in a simulation which suggest that both bonus and tenure policies outlined in his paper have greater benefits than costs, though he acknowledges that these analyses are based on hypothesized parameters that the field has not yet estimated well. Indeed, this may depend very much on local labor market conditions.

One final but important concern with policies that attempt to predict future performance based on imperfect information from the early career is potentially non-random error in measurement. If value-added measures used to detect early performance might systematically favor one group of teachers over another based on characteristics unrelated to true effectiveness. For example, value-added scores could be lower for teachers working in disadvantaged schools or with certain student populations. Most research on value-added shows relatively small systematic bias of this type but the research is likely incomplete (Raudenbush, 2013). It is also possible some group of teachers has lower value-added but greater effectiveness on a different dimension of teaching. If this were the case then if the use of value-added discouraged teachers with these other important skills from teaching, then the teaching force could suffer. More generally, narrowly defined measures of quality could reduce the diversity of teaching force along multiple dimensions.

As a first attempt to explore this concern, we examine the racial/ethnic breakdown of teachers at different points in the distribution of initial effectiveness (again, according to a

teacher's mean value-added in the first two years). We examine characteristics of teachers who are in the extremes of the initial performance distribution—that is, the top 5 and 10 percent (the initially highest performers), as well as the bottom 5 and 10 percent. This analysis, unlike analyses elsewhere in this paper, include all teachers for whom we are able to calculate initial performance (value-added in the first two years of teaching) because the question is whether early career identification disproportionately affects teachers by race/ethnicity. Table 5 gives the relative percentages of teachers identified at each of these thresholds are quite similar by race The differences for both math and ELA are small and never statistically significantly different from each other.[12] These findings suggest that a policy of identification of early career teachers by value-added scores would not incidentally identify minority teachers at differential rates as either high or low performers, at least in the case of New York City.

Conclusions

From a policy perspective, the ability to predict future performance is most useful for inexperienced teachers because policies that focus on retention, development (e.g. mentoring programs), tenure, dismissal, and promotion are likely most relevant during this period. In this paper we describe the trajectory of teachers' performance over their first five years as measured by their value-added to math and ELA test scores of students. Our goal is to assess the potential for predicting future performance (performance in years 3, 4, and 5) based on teachers' performance in their first two years. We find that, on average, initial performance is predictive of future performance, far more so than measured teacher characteristics such as their own test performance (e.g. SAT) or education. On average the highest fifth of teachers remain the highest fifth of teachers; the second fifth remains the second fifth; and so on. Predictions are more

powerful at the extremes of the performance distribution, and also in math relative to ELA. Finally, it appears to be somewhat easier to identify teachers who will be excellent in the future, as opposed to teachers who will be very ineffective.

This said, predictions about teachers' future performance based on initial value-added are far from perfect. Initial performance accounts for about 25 percent of the overall variance in future math performance and 16 percent in future ELA performance. Thus, basing human resource decisions on initial value-added estimates will lead to errors since some teachers who would, in fact, be highly effective will be treated as ineffective, and some teachers who would be ineffective, will be treated as if they were effective. However, it is important to keep in mind that most districts have a default policy in which they make little attempt in the first few years to use value-added information to anticipate future effectiveness. This *absence* of policy also inherently misidentifies teachers: In this instance, identification rates are zero—no teachers are judged to be ineffective when in fact some do turn out to be relatively low-performing. The costs of these mistakes by omission are typically not discussed and are born by students who are subjected to less effective teachers who could have been identified for intervention early in their careers. The relevant question for educational policy is not whether predictions of teacher effectiveness misidentify teachers—any prediction of human behavior will inevitably contain errors—but rather what is the level of identification that maximizes the net benefits? Is it nearly zero, which is the default policy in many districts, or some level above that?

Ultimately that is a question that policymakers must resolve as they weigh benefits and costs of alternative levels of identifying high- and low-performing teachers in their state or district. Crucial to that decision is an empirical understanding of the accuracy of alternative predictions. Our data from New York City suggest that at relatively low levels of identifying

teachers, e.g. the bottom and top 5 percent, initial performance accurately categorizes future performance for most math teachers (about 75 percent), but for ELA teachers predictions are closer to being accurate about half the time. Compare this to a district which makes no attempt to identify struggling teachers at the start of their careers and therefore makes no accurate predictions about future ineffective teachers. Even 50 percent accuracy seems an improvement over making no predictions at all.

At the same time, it is important to acknowledge that any policy based on value-added scores would necessarily be limited to the 20 to 30 percent of district employees who possess value-added scores in multiple years, and then on top of that, it would at most identify a small subset of those teachers (we discuss herein identification rates of 5 to 10 percent, but this would depend on the given policy). One the one hand, if it is the case that only 8 percent of the 5 percent who are initially identified are *mis*-identified (as we find in math), then one positive note is that very few teachers overall would experience this misclassification. On the other hand, the benefits of correctly identifying teachers early in their career is also necessarily limited to a subset of that small group of 5 to 10 percent of teachers. Depending on how productively a district can respond to a teacher's early identification (can we help them improve? can we recruit better replacements?), the evaluation system may not have a large impact on the overall distribution of teaching effectiveness. Given that these systems are controversial and not always favored by teachers, it is unclear whether the overall benefits are worth the costs. That said, for the set of students who are assigned to teachers that the district could have predicted would continue to struggle, the intervention might be quite valuable.

Finally, it is also important to acknowledge that the stability of value-added scores could vary from district-to-district (McCaffrey et al., 2009), which in turn could mean that the

predictive power could be stronger or weaker in other places. Therefore districts may be interested in implementing their own analyses of the predictive power of the teaching effectiveness measures as an informative step to shaping policies based on those measures.

Tables

Table 1:
Population of Teachers Who Began Teaching in SY 1999-00 or after and Primarily Taught Grades 4 and 5: Descriptive Statistic on Three Relevant Analytic Samples Restrictions

Has VA Scores in At Least...	Math (A) 1st Year	Math (B) .. And 2 of Next 4 Yrs	Math (C) Years 1 thru 5	ELA (A) 1st Year	ELA (B) .. And 2 of Next 4 Yrs	ELA (C) Years 1 thru 5
Average Value-Added Score in First Year	-0.035	-0.032	-0.030	-0.036	-0.034	-0.030
Proportion Female	84.6%	85.2%	85.9%	84.6%	85.3%	86.0%
Proportion White	63.3%	63.1%	65.3%	64.1%	64.1%	66.4%
Proportion Black	17.5%	17.7%	17.8%	17.8%	18.2%	18.3%
Proportion Hispanic	11.5%	11.6%	10.3%	10.6%	10.5%	9.1%
Average Standardized Verbal SAT Score	-0.107	-0.124	-0.120	-0.108	-0.129	-0.126
Average Standardized Math SAT Score	-0.100	-0.123	-0.145	-0.110	-0.137	-0.148
Proportion Attended Most Competitive UG	11.8%	10.7%	9.7%	11.3%	10.3%	9.1%
Proportion Attended Competitive UG	17.9%	18.3%	19.9%	18.2%	18.7%	20.5%
Proportion Attended Less Competitive UG	39.6%	40.2%	40.7%	40.2%	40.9%	41.8%
Proportion Attended Not Competitive UG	22.9%	23.8%	24.5%	22.6%	23.3%	23.8%
Proportion Attended Unknown UG	7.8%	7.1%	5.2%	7.7%	6.8%	4.7%
Pathway into Tching= College Recommended Path	54.0%	55.7%	56.7%	54.3%	56.1%	57.4%
Pathway into Tching= TFA Path	1.6%	0.7%	0.1%	1.6%	0.9%	0.2%
Pathway into Tching= Other Non-Traditional Path	23.9%	24.3%	27.0%	23.8%	24.1%	26.4%
Pathway into Tching= Unknown Path	8.8%	8.4%	8.2%	8.7%	8.2%	7.3%
Number of Teachers	**3360**	**2333**	**966**	**3307**	**2298**	**972**

Table 2:
Cross Year Correlation of Value-Added for Early Career Teachers and Veteran Teachers,

	Math			**ELA**		
	Novice (Exp=1)	**Veteran (Exp > 5)**	**P-Value**	**Novice (Exp=1)**	**Veteran (Exp > 5)**	**P-Value**
Year +1	0.356	0.421	0.000 ***	0.206	0.293	0.000 ***
Year +2	0.302	0.384	0.000 ***	0.160	0.258	0.000 ***
Year +3	0.275	0.333	0.003 ***	0.131	0.207	0.010 **
Year +4	0.191	0.321	0.000 ***	0.090	0.171	0.018 *
Year +5	0.132	0.321	0.000 ***	0.152	0.185	0.049 *

Notes: The columns for Experience = 1 are the correlations of teachers' first year value-added with their value-added in subsequent five years (five rows). The columns for Experience > 5 are the correlations for teachers with at least six years of experience with their value-added in the subsequent five years. The p-values reported above are for the statistical test that the correlations for novice versus veteran teachers are statistically different from one another.

Table 3:
Adjusted R-Squared Values for Regressions Predicting Future (Years 3, 4, and 5) VA Scores
as a Function of Sets of Value-Added Scores from the First Two Years

	Outcome			
Early Career VA Predictor(s)	VA in Y3	VA in Y4	VA in Y5	Mean(VA$_{Y3-5}$)
Math				
Math VA in Y1 Only	0.079	0.052	0.077	0.111
Math VA in Y2 Only	0.153	0.149	0.117	0.223
Math VA in Y1 & Y2	0.176	0.158	0.146	0.256
VA in Both Subjects in Y1 & Y2	0.176	0.171	0.147	0.262
VA in Both Subjects in Y1 & Y2 (cubic)	0.178	0.171	0.146	0.261
ELA				
ELA VA in Y1 Only	0.025	0.019	0.016	0.040
ELA VA in Y2 Only	0.058	0.080	0.042	0.117
ELA VA in Y1 & Y2	0.068	0.084	0.048	0.131
VA in Both Subjects in Y1 & Y2	0.085	0.102	0.058	0.161
VA in Both Subjects in Y1 & Y2 (cubic)	0.090	0.113	0.061	0.168

Table 4:
Quintile Transition Matrix from Initial Performance to Future Performance, By Subject
(Number, Row Percentage, Column Percentage)

|		Quintile of Future Math Performance					
Math Initial Quintile		Q1	Q2	Q3	Q4	Q5	Row
Q1	n	47	47	26	25	7	152
	(row %)	(30.9)	(30.9)	(17.1)	(16.4)	(4.6)	
	(col %)	(39.8)	(24.7)	(11.2)	(10.6)	(3.6)	
Q2	n	28	47	60	33	16	184
	(row %)	(15.2)	(25.5)	(32.6)	(17.9)	(8.7)	
	(col %)	(23.7)	(24.7)	(25.8)	(14.0)	(8.2)	
Q3	n	24	47	44	59	34	208
	(row %)	(11.5)	(22.6)	(21.2)	(28.4)	(16.3)	
	(col %)	(20.3)	(24.7)	(18.9)	(25.0)	(17.3)	
Q4	n	14	32	58	64	46	214
	(row %)	(6.5)	(15.0)	(27.1)	(29.9)	(21.5)	
	(col %)	(11.9)	(16.8)	(24.9)	(27.1)	(23.5)	
Q5	n	5	17	45	55	93	215
	(row %)	(2.3)	(7.9)	(20.9)	(25.6)	(43.3)	
	(col %)	(4.2)	(8.9)	(19.3)	(23.3)	(47.4)	
Column Total		118	190	233	236	196	**973**
		Quintile of Future ELA Performance					
ELA Initial Quintile		Q1	Q2	Q3	Q4	Q5	Row
Q1	n	49	51	44	26	16	186
	(row %)	(26.3)	(27.4)	(23.7)	(14.0)	(8.6)	
	(col %)	(39.2)	(25.1)	(19.0)	(11.0)	(8.6)	
Q2	n	31	40	45	40	22	178
	(row %)	(17.4)	(22.5)	(25.3)	(22.5)	(12.4)	
	(col %)	(24.8)	(19.7)	(19.5)	(16.9)	(11.9)	
Q3	n	19	52	44	58	31	204
	(row %)	(9.3)	(25.5)	(21.6)	(28.4)	(15.2)	
	(col %)	(15.2)	(25.6)	(19.0)	(24.5)	(16.8)	
Q4	n	13	41	48	59	47	208
	(row %)	(6.3)	(19.7)	(23.1)	(28.4)	(22.6)	
	(col %)	(10.4)	(20.2)	(20.8)	(24.9)	(25.4)	
Q5	n	13	19	50	54	69	205
	(row %)	(6.3)	(9.3)	(24.4)	(26.3)	(33.7)	
	(col %)	(10.4)	(9.4)	(21.6)	(22.8)	(37.3)	
Column Total		125	203	231	237	185	**981**

Table 5:
Identification of Top and Bottom Performers by Race/Ethnicity and Subject
(column percentages)

	Initial Percentage Identified		**White**	**Black**	**Hispanic**
Math	top	5%	5.37	5.67	5.00
	top	10%	9.73	11.17	10.00
	bottom	5%	4.44	4.50	4.77
	bottom	10%	9.44	6.67	11.36
ELA	top	5%	5.69	4.83	5.58
	top	10%	9.89	10.50	9.90
	bottom	5%	4.79	3.83	4.82
	bottom	10%	9.59	8.67	8.63

Note: Unlike other tables in the paper, this sample is *not* restricted to the set of teachers who have value-added in all of their first five years. Because this analysis only relies on knowledge of value-added in first two years, the sample is only restricted to the set of teachers who have value-added in the first two years of teaching. Omitted from this table are teachers of other races, which in total constitute 5.2 percent of the sample.

Figure 1:
Student Achievement Returns to Teacher Early Career Experience, Preliminary Results from Current Study (Bold) and Various Other Studies
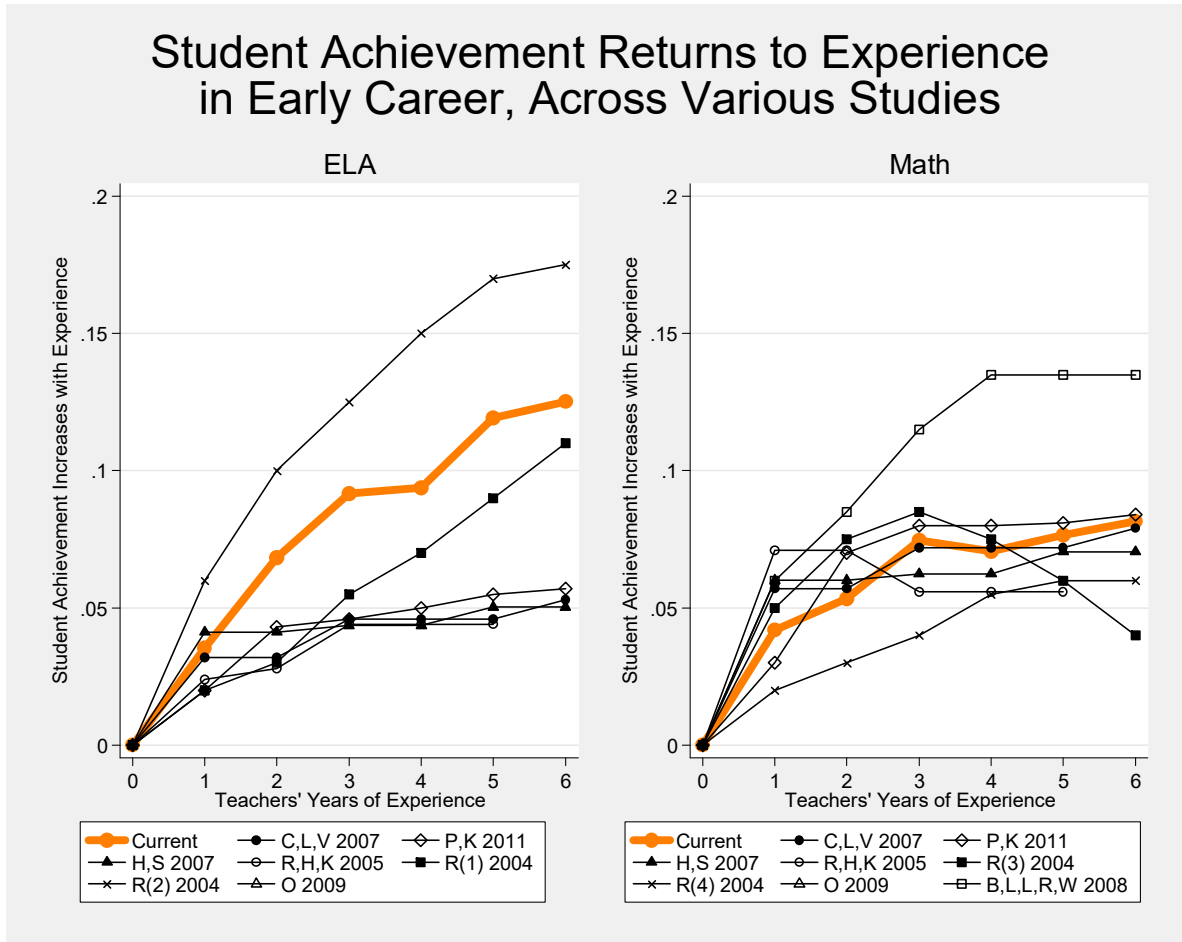
Results are not directly comparable due to differences in grade level, population, and model specification, however Figure 1 is intended to provide some context for estimated returns to experience across studies for our preliminary results. Current= Results for grade 4 & 5teachers who began in 2000+ with at least 9 years of experience. For more on model, see Technical Appendix. C,L V 2007= = Clotfelter, Ladd, Vigdor (2007; Rivkin, Hanushek, & Kain, 2005), Table 1, Col. 1 & 3; P, K, 2011 = Papay & Kraft (2011), Figure 4 Two-Stage Model; H, S 2007 = Harris & Sass (2011), Table 3 Col 1, 4 (Table 2); R, H, K, 2005= Rivkin, Hanushek, Kain (2005), Table 7, Col. 4; R(A-D) 2004 = Rockoff (2004), Figure 1 & 2, (A= Vocab, B= Reading Comprehension, C= Math Computation, D= Math Concepts); O 2009 = Ost (2009), Figures 4 & 5 General Experience; B,L,L,R,W 2008 = Boyd, Lankford, Loeb, Rockoff, Wyckoff (2008).

Figure 2:
Mean VA Scores, by Subject (Math or ELA), Quintile of Initial Performance, and Years of Experience for Elementary School Teachers with VA Scores in at Least First Five Years of Teaching.

Experience Required= (observed at least 1st 05 years with VA)
Quintiles Of Mean of First 2 Years
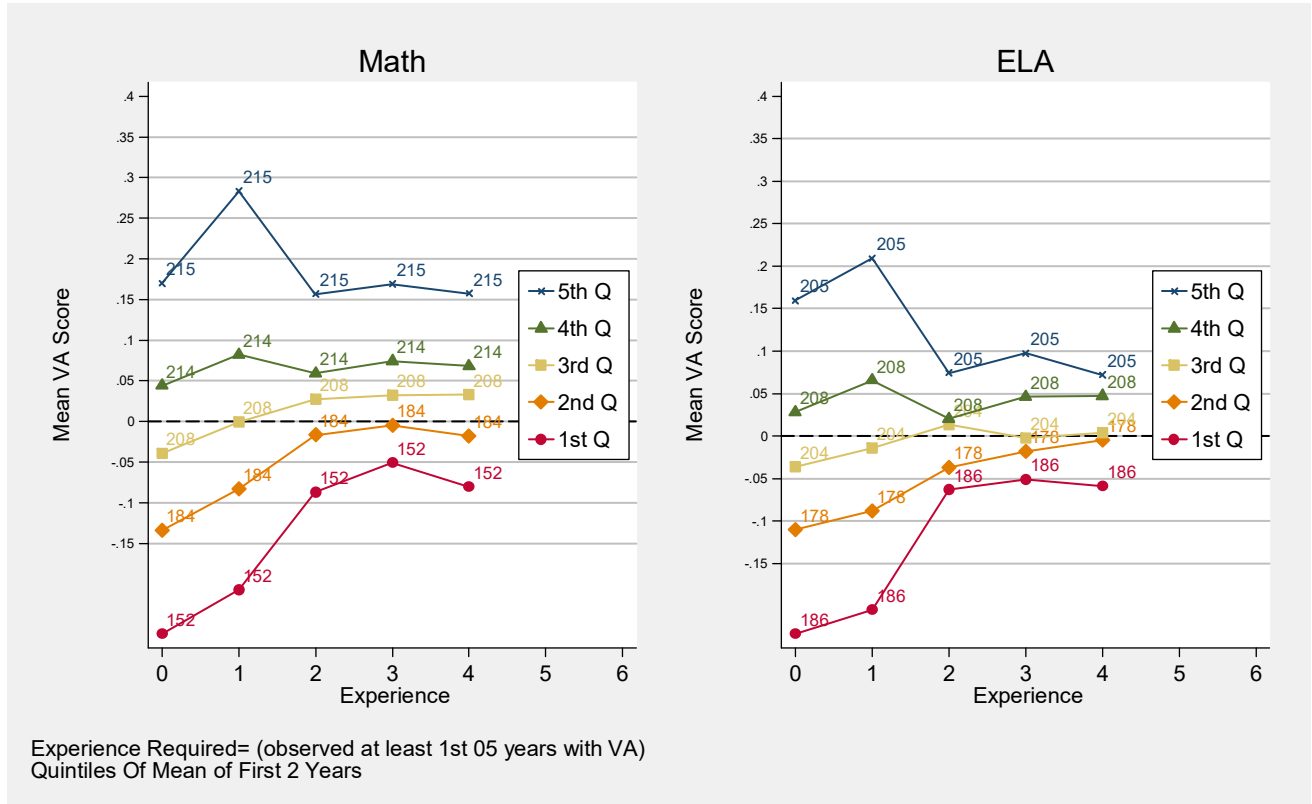
FN: Numbers at each time point are sample sizes. These reflect the fact that quintiles are defined before limiting the sample to teachers with value-added in all of their first five years. The sample sizes also reinforce the fact that patterns observed over time are among a consistent sample—changes over time are not due to any non-random attrition. The issues of defining quintiles and sample selection are discussed in greater detail in Appendices A and C.

Distribution of Future Value-Added Scores, by Initial Quintile of Performance

Math Mean VA Score in Years 3, 4, & 5, by Initial Quintiles

Experience Required= (observed at least 1st 05 years with VA)
Quintiles Of Mean of First 2 Years

Math Future Effectiveness
(Mean VA Score in Years 3, 4, & 5 of Experience)

Legend:
- Q1 (152), Future Mean, Initial Mean
- Q2 (184), Future Mean, Initial Mean
- Q3 (208), Future Mean, Initial Mean
- Q4 (214), Future Mean, Initial Mean
- Q5 (215), Future Mean, Initial Mean

ELA Mean VA Score in Years 3, 4, & 5, by Initial Quintiles

Experience Required= (observed at least 1st 05 years with VA)
Quintiles Of Mean of First 2 Years

ELA Future Effectiveness
(Mean VA Score in Years 3, 4, & 5 of Experience)

Legend:
- Q1 (186), Future Mean, Initial Mean
- Q2 (178), Future Mean, Initial Mean
- Q3 (204), Future Mean, Initial Mean
- Q4 (208), Future Mean, Initial Mean
- Q5 (205), Future Mean, Initial Mean

Figure 4: Depiction of Error Rate for Initially Identifying a Percentage of Teachers as Low-Performing Based on Initial Value-Added Scores in the First Two Years, by Subject
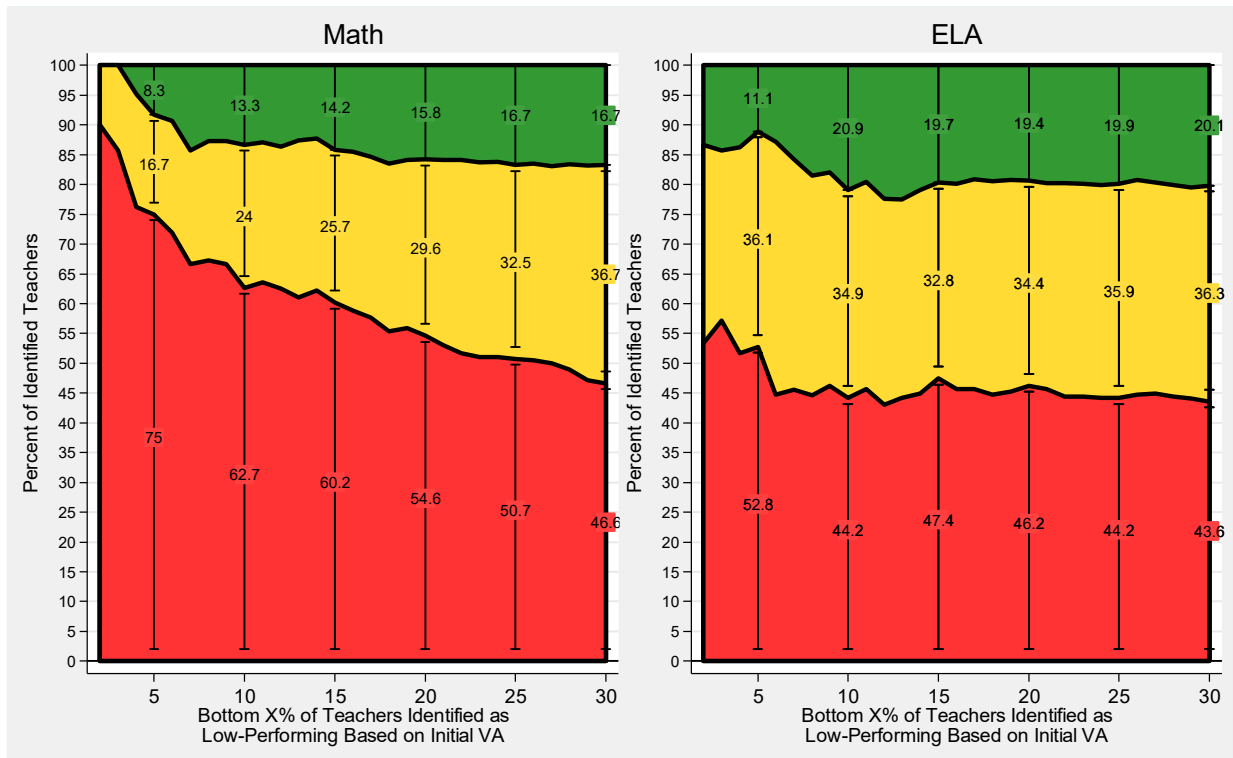
Appendix A

The most straightforward approach to making quintiles would be to simply break the full distribution of teacher-by-year fixed effects into five groups of equal size. However, we know that value-added scores for first year teachers are, on average, lower than value-added scores for teachers with more experience. For the purposes of illustration, imagine that first year teacher effects comprise the entire bottom quintile of the full distribution. In this case, we would observe no variability in first year performance—that is, all teachers would be characterized as "bottom quintile" teachers, thus eliminating any variability in initial performance that could be used to predict future performance. We thus choose to center a teacher's first year value-added score around the mean value-added for first year teachers and then created quintiles of these centered scores. By doing so, quintiles captured whether a given teacher was relatively more or less effective than the average *first* year teacher, rather than the average teacher in the district.

In order to trace the development of teachers' effectiveness over their early career, we limited the analytic sample to teachers with a complete set of value-added scores in the first five years. As is evident from Table 1 in the paper, about 29 percent of elementary teachers with value-added scores in their first year meet this restrictive inclusion criterion. We hesitated to first restrict the sample and then make quintiles solely within this small subset, because we observed that teachers with a more complete value-added history tended to have higher initial effectiveness. In other words, a "bottom quintile" first year teacher in the distribution of teachers with at least five consecutive years of value-added might not be comparable to the "bottom quintile" among all first years teachers for whom we might wish to make predictions. For this reason, we made quintiles relative to the sample of all teachers regardless of the number of value-added scores they possessed, and subsequently limited the sample to those with at least

five years of value-added. As a result of this choice, we observe slightly more top quintile teachers than bottom quintile teachers in the initial year. However by making quintiles before limiting the sample, we preserve the absolute thresholds for those quintiles and thus ensure that they are consistent with the complete distribution of new teachers. In addition, it is simply not feasible for any districts to make quintiles in the first year or two depending on how many value-added scores *will* have in the first five years.

Finally, our ultimate goal is to use value-added information from the early career to produce the most accurate predictions of future performance possible. Given the imprecision of any one year of value-added scores, we average a teacher's value-added scores in years one and two and make quintiles thereof. In Appendix C, we present some specification checks by examining our main results using value-added from the first two years in a variety of ways (e.g., first year only, second year only, a weighted average of the first two years, teachers who were consistently in the same quintile in both years). In Appendix Table A1 below, we present the number of teachers and mean of value-added scores in each of five quintiles of initial performance, based on these various methods for constructing quintiles. One can see that the distribution of the teachers in the analytic sample (fourth and fifth grade teachers with value-added scores in first five years) depends on quintile construction.

Appendix Table A1:
Analytic Sample: 966 Teachers Who Have Value-Added Scores in all of First Five Years.
Difference in Mean Value Added and Numbers of Final Analytic Sample Teachers in each Quintile of Initial Performance, Depending on Approach to Quintile Construction

Approach to Quintile Construction		Q1	Q2	Q3	Q4	Q5	Total
Math							
Quintiles of All Teacher-Years (1)	n	224	207	194	219	122	966
	mean	-0.165	-0.049	0.015	0.092	0.222	
Quintiles Made After Limiting to Teachers in First Year (2)	n	171	171	198	212	214	966
	mean	-0.224	-0.100	-0.018	0.063	0.227	
...And Limiting to Elementary Teachers (3)	n	150	187	207	213	209	966
	mean	-0.235	-0.107	-0.018	0.065	0.230	
… And Limiting to Teachers with 5+ VA score (4)	n	194	193	193	193	193	966
	mean	-0.214	-0.083	-0.002	0.077	0.239	
ELA							
Quintiles of All Teacher-Years (1)	n	246	196	208	181	141	972
	mean	-0.156	-0.059	0.002	0.066	0.158	
Quintiles Made After Limiting to Teachers in First Year (2)	n	214	163	185	198	212	972
	mean	-0.206	-0.088	-0.022	0.046	0.180	
...And Limiting to Elementary Teachers (3)	n	185	176	201	208	202	972
	mean	-0.217	-0.098	-0.025	0.048	0.185	
… And Limiting to Teachers with 5+ VA score (4)	n	195	194	195	194	194	972
	mean	-0.213	-0.090	-0.016	0.054	0.188	

Note: We construct quintiles of performance in a teacher's first two years. The final analytic sample of teachers is restricted to the teachers who taught primarily fourth or fifth grade and for whom we observe at least five consecutive years of VA scores, beginning in the teacher's first year of teaching. Note that method (3) above is the preferred approach for this paper.

Appendix B

Estimation of Teacher Value-Added

We estimate teacher-by-year value-added employing a multi-step residual-based method similar to that employed by the University of Wisconsin's Value-Added Research Center (VARC). VARC estimates value-added for several school districts, including until quite recently New York City.

We initially estimate equation 1, which regresses achievement (Y_{icsjt}) for student i in class c at school s taught by teacher j in time t as a function of prior achievement ($Y_{icsjt-1}$), student attributes (X_{icsjt}), and class fixed effects (α_{csjt}). In this model, the class fixed effects subsumes both the teacher-by-year fixed effect (τ_{jt}) and any other class (Z_{csjt}) or school-level (S_{st}) predictors of student achievement.

$$Y_{icsjt} = \lambda Y_{icsjt-1} + \beta' X_{icsjt} + \alpha_{csjt} + \varepsilon_{icsjt} \qquad (1)$$

$$\text{where } \alpha_{csjt} = \gamma' Z_{csjt} + \varphi' S_{st} + \tau_{jt}$$

Employing these estimates, we calculate the residuals ($\hat{\varepsilon}_{icsjt}$) from this regression without accounting for α_{csjt} and then estimate equation 2 which regresses this residual on class and school characteristics as well as a class random effect (ζ_{jt}) to reflect the grouping of students into classrooms.

$$\hat{\varepsilon}_{icsjt} = \alpha_{csjt} + \varepsilon_{icsjt} = \gamma' Z_{csjt} + \varphi' S_{st} + \zeta_{jt} + \omega_{icsjt} \qquad (2)$$

Employing these estimates, we calculate the residuals (q_{icsjt}) from this model and calculate teacher-by-year value-added by averaging across the student-level residuals within a teacher and year.

$$\hat{\tau}_{jt} = \bar{q}_{icsjt} \qquad (3)$$

The teacher-by-experience fixed effects become the value-added measures which serve as the outcome variable in our later analyses. They capture the average achievement of teacher j's students in year t, conditional on prior skill and student characteristics, relative to the average teacher in the same subject and grade. Finally, we apply an Empirical Bayes shrinkage adjustment to the resulting teacher-by-year fixed effect estimates to adjust for measurement error.

The standard errors of the teacher-by-year value-added estimates are estimated as shown in equation 4 using the student-level errors ($e_{icsjt} = q_{icsjt} - \hat{\tau}_{jt}$) from equation 3 and number of observations for each teacher-by-year group.

$$SE(\hat{\tau}_{jt}) = \sqrt{var(e_{icsjt}) \Big/ N_{jt}} \qquad (4)$$

We then employ a standard Empirical Bayes shrinkage method to account for the varying uncertainty associated with each teacher-by-year value-added estimate.

In the teacher-by-year value-added model presented above we make several important analytic choices about model specification. Our preferred model uses a lagged achievement as opposed to modeling gain scores as the outcome).[xiii] The model attends to student sorting issues through the inclusion of all available student covariates rather than using student fixed effects, in part because the latter restricts the analysis to comparisons only between teachers who have taught at least some students in common.[xiv] At the school level we also opt to control for all observed school-level covariates that might influence the outcome of interest rather than including school fixed effects, since this would also only allow valid comparisons within the same school. In an appendix, we examine results across a variety of value-added models, including models with combinations of gain score outcomes, student, and school fixed effects.

Appendix C

In Figure 2 of the paper, we present mean value-added scores over the first five years of experience, by initial performance quintile. We do so on a somewhat restrictive sample of about 29 percent of the elementary teachers with value-added scores in their first year teaching who *also* have value-added scores in all of their first five years (see Table 1). As discussed in the paper, we also rerun analyses on a less restrictive sample of teachers who have value-added scores in only two of the four years following their first. This is but one example of an analytic choice made in this paper that could affect our findings. In this Appendix, we examine whether our primary findings are robust to three analytic choices made in the paper: (A) minimum value-added required for inclusion in the sample, (B) how we defined initial quintiles, and (C) specification of the value-added models used to estimate teacher effects:

(A) We examine results across two teacher samples based on minimum value-added required for inclusion. The first figure uses the analytic sample used throughout the main paper—teachers with value-added scores in all of their first five years. The second widens the analytic sample to the set of teachers who are consistently present in the dataset for at least five years, but only possess value-added scores in their 1st , and 2 of the next 4 years.

(B) We examine results across four possible ways of defining quintiles: (1) "Quintile of First Year"—this is quintiles of teachers' value-added scores in their first year alone; (2) "Quintile of the Mean of the First Two Years"—this is quintiles of teacher's *mean* value-added scores in the first *two* years and is the approach we use throughout the paper; (3) "Quintile Consistent in First Two Years"—here we group teachers who were consistently in the same quintiles in first and second year (i.e., top quintile both years); and (4) "Quintile of the Mean of

Y1, Y2, & Y2"—the quintiles of teacher's mean value added score in first and second year, double-weighting the second year.

(C) Finally, we examine results using two alternative value-added models to the one used in the paper. "VA Model B" uses a gain score approach rather than the lagged achievement approach used in the paper. "VA Model D" differs from the main value-added model described in the paper in that it uses student-fixed effects in place of time-invariant student covariates such as race/ ethnicity, gender, etc. See next page for results.

Elem Teachers with VAM in All of First Five Years
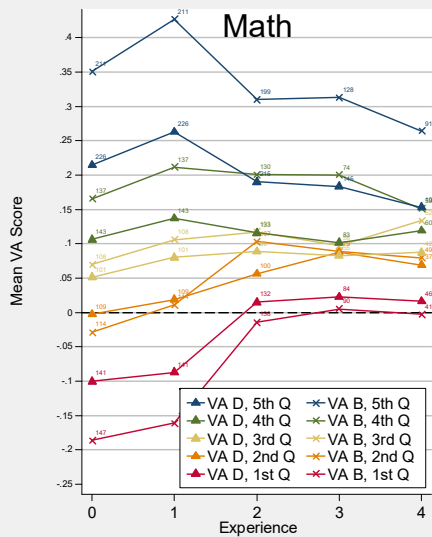
Elem Teachers with VAM in 1st, and 2 of Next 4 Years

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Endnotes

[1] Results are not directly comparable due to differences in grade level, population, and model specification, however Figure 1 is intended to provide some context for estimated returns to experience across studies for our preliminary results.

[2] A one standard deviation increase in teacher effectiveness is typically 15 to 20 percent of standard deviation of student achievement. See Hanushek, Rivkin, Figlio, & Jacob (2010) for a summary of studies that estimate the standard deviation of teacher effectiveness measures in terms of student achievement. The estimates for Reading are between 0.11 and 0.26 standard deviations across studies, while the estimates for math are larger and also exhibit somewhat more variability (0.11 to 0.36, but with the average around 0.18 standard deviations (Aaronson, Barrow, & Sander, 2007; Hanushek & Rivkin, 2010; Jacob & Lefgren, 2008; Kane, Rockoff, & Staiger, 2008; Thomas J. Kane & D.O. Staiger, 2008; Koedel & Betts, 2011; Nye, Konstantopoulos, & Hedges, 2004; Rivkin et al., 2005; Rockoff, 2004; Rothstein, 2010).

[3] We form quintiles of initial performance employing the average of the first two years of value-added. See Appendix for a series of checks using different samples of teachers based on minimum years of value-added scores required, definitions of initial performance quintiles, and specifications of the value-added model.

[4] These results are available from the authors upon request.

[5] We use the mean of years 3, 4, and 5 rather than just the fifth year to absorb some of the inherently noisy nature of value-added scores over time.

[6] The value-added scores depicted in each distribution are each teacher's mean value-added score in years three, four, and five. For brevity, we refer to these scores as "future" performance.

[7] For example, typical policy discussions of top and bottom performers often reference 5 to 10 percent of teachers (see, e.g., Hanushek (2011)).

[8] In this example, we categorize a teacher in the bottom third of performance as generally low-performing. Any percentile of future performance could be employed to identify low-performance. In our example, the most effective teacher in the bottom tercile performs at a level below that of the average new teacher. The selection of a percentile threshold for future low performance has implications for the precision of the estimates. If that percentile was the 25th rather than the 33rd, then we would be more restrictive in our definition of future performance and thus misidentify a higher proportion of teachers. The same implications hold for misidentification of high-performing teachers.

[9] The inherent tensions associated with performance-based identification of teachers are present with identification of any segment of teachers for any purpose, although as we show below the consequences of identification likely influence how we weigh the costs of misidentification.

[10] It is important to note that, some of these "misidentified" teachers are still performing below average in the future. Therefore, even some of the misidentified teachers could benefit from some human capital intervention.

[11] Though we are imagining an alternative policy scenario we think it quite realistic—many districts today do not use value-added scores formally as part of evaluation—it is still the case that the mere availability of these measures could encourage some teachers to self-select out of the profession, or for some teachers to be informally counseled out. Therefore, even if there is no formal policy that ties performance measures to teacher retention, there could be some informal sorting based on value-added. It is also worth mentioning that most districts do tend to have systems for identifying teachers for dismissal, however given tenure policies this tends to be a very small group of teachers.

[12] In a separate analysis (not shown), we conduct a similar analysis examining the racial breakdown by initial performance, however we separate results across all five quintiles of the distribution of initial performance, rather than simply the top/ bottom 5, 10, 15, and 20 percent. The findings are similar: There is no evidence that minority teachers are more likely to appear in lower quintiles—there are only slight fluctuations in the racial/ demographic breakdown of quintiles but for black and Hispanic teachers there is no clear pattern in those fluctuations. Results are available upon request.

[xiii] Some argue that the gain score model is preferred because one does not place any prior achievement scores which are measured with error on the right-hand side, which introduces potential bias. On the other hand, the gain score model has been criticized because there is less variance in a gain score outcome and a general loss of information and heavier reliance on the assumption of interval scaling. In addition, others have pointed out that the gain score model implies that the impacts of interest persist undiminished rather than directly estimating the relationship between prior and current year achievement (McCaffrey, Lockwood, Koretz, Louis, & Hamilton, 2004; McCaffrey et al., 2009).

[xiv] A student fixed effects approach has the advantage of controlling for all observed and unobserved time-invariant student factors, thus perhaps strengthening protections against bias. However, the inclusion of student-level fixed effects entails a dramatic decrease in degrees of freedom, and thus a great deal of precision is lost (see discussion in McCaffrey et al., 2009). In addition, experimental research by Kane and Staiger (2008) suggests that student fixed effects estimates may be *more* biased than similar models using a limited number of student covariates.